

$$f(z) = z^2 \quad z = x + yi$$

$$z^2 = (x + yi)^2 = x^2 - 2xyi - y^2$$

$$\operatorname{Re} z^2 = x^2 - y^2 \quad \operatorname{Im} z^2 = -2xy$$